

Name: _____

Topic: _____

For the student to
 complete at home
 (if possible)

Fill in squares (a)

$$100^2 = \dots$$

Use the grid below to find the first square number which is the sum of two consecutive odd numbers. Use the grid below to find the first square number which is the sum of two consecutive even numbers. Use the grid below to find the first square number which is the sum of two consecutive odd numbers. Use the grid below to find the first square number which is the sum of two consecutive even numbers.

The grid of 100 squares below is divided into four equal quadrants. Use the grid to find the first square number which is the sum of two consecutive odd numbers. Use the grid to find the first square number which is the sum of two consecutive even numbers. Use the grid to find the first square number which is the sum of two consecutive odd numbers. Use the grid to find the first square number which is the sum of two consecutive even numbers.

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will proceed through an equilibrium

precipitation of $\text{Al}(\text{OH})_3$ and $\text{Fe}(\text{OH})_3$

at pH 7.5, the concentration of Al^{3+} and Fe^{3+} will be very low, and the concentration of $\text{Al}(\text{OH})_3$ and $\text{Fe}(\text{OH})_3$ will be high.

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Thus, the precipitation of $\text{Al}(\text{OH})_3$ and $\text{Fe}(\text{OH})_3$ will be favored at pH 7.5.



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(b) $\frac{d^2y}{dx^2} = 0$ at $x = 0$ and $x = 2$.
 (c) $\frac{d^2y}{dx^2} < 0$ at $x = 1$ and $x = 3$.
 (d) $\frac{d^2y}{dx^2} > 0$ at $x = 0$ and $x = 2$.

The function $y = f(x)$ is continuous on the interval $[0, 4]$ and has a local maximum at $x = 1$ and a local minimum at $x = 3$.

Which of the following is a possible graph of $y = f(x)$ on the interval $[0, 4]$?

(A)

(B)

(C)

(D)

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(A)

Integrated by inspection (2) we get

$$\frac{1}{2} \ln \left| \frac{y_2}{y_1} \right| + \frac{1}{2} \ln \left| \frac{y_1}{y_2} \right| = 0$$

we get $\ln \left| \frac{y_2}{y_1} \right| + \ln \left| \frac{y_1}{y_2} \right| = 0$ (3)

which is the same as $\ln \left| \frac{y_2}{y_1} \cdot \frac{y_1}{y_2} \right| = 0$

which is just $\ln |1| = 0$ by inspection the constant we get through this finding there must be $\frac{1}{2} \ln \left| \frac{y_2}{y_1} \right| = -\frac{1}{2} \ln \left| \frac{y_1}{y_2} \right|$



From the graph, it is obvious

for the constant $\ln \left| \frac{y_2}{y_1} \right| = 0$ regarding that the domain of \ln function is the positive values, and $\frac{y_2}{y_1}$ constant with domain the domain.

Therefore (2) can be integrated between the limits y_1 and y_2 as $\int_{y_1}^{y_2} \frac{1}{y} dy = \ln \left| \frac{y_2}{y_1} \right|$

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$$\int_{y_1}^{y_2} \frac{1}{y} dy = \ln \left| \frac{y_2}{y_1} \right| \quad \text{---(5)}$$

$$\int_{y_1}^{y_2} \frac{1}{y} dy = \ln \left| \frac{y_2}{y_1} \right| \quad \text{---(6)}$$

From this diagram, the level of income tax is determined by the value of expenditure (income) Y_2 and Y_1 in comparison to the Y_0 tax base and the rates.

and (iii) together in terms of Y_2 the income tax T_2 and T_1 are related in such a way by the relation:

$$T_2 = T_1 + Y_2 - Y_1$$

Using equation (ii) we get:

$$T_2 - T_1 = Y_2 - Y_1 + Y_1 - Y_1$$

The corresponding increase in tax revenue $T_2 - T_1$ is equal to the

$$\frac{d(T_2 - T_1)}{dY_2} = \frac{dT_2}{dY_2} - \frac{dT_1}{dY_2} = \frac{dT_2}{dY_2}$$

or $\frac{dT_2}{dY_2} = \frac{dT_1}{dY_2} + \frac{d(Y_2 - Y_1)}{dY_2}$

But from equation (ii) we have $\frac{dT_1}{dY_2} = \frac{dT_1}{dY_1} \cdot \frac{dY_1}{dY_2}$ and we put the value for every respective rate

$$\frac{dT_2}{dY_2} = \frac{dT_1}{dY_1} \cdot \frac{dY_1}{dY_2} + \frac{d(Y_2 - Y_1)}{dY_2}$$

$$\frac{dT_2}{dY_2} = \frac{dT_1}{dY_1} \cdot \frac{dY_1}{dY_2} + \frac{dY_2 - dY_1}{dY_2}$$

Let us assume that $\frac{dY_1}{dY_2} = \frac{1}{2}$ and $\frac{dT_1}{dY_1} = \frac{1}{3}$

$$\frac{dT_2}{dY_2} = \frac{1}{3} \cdot \frac{1}{2} + \frac{dY_2 - \frac{1}{2}dY_2}{dY_2} = \frac{1}{6} + \frac{\frac{1}{2}dY_2}{dY_2} = \frac{1}{6} + \frac{1}{2} = \frac{2}{3}$$

Thus, the increase in tax revenue is equal to the

change in income Y_2 multiplied by the average tax rate on Y_2 .

Thus, we can say that the average tax rate on Y_2 is equal to the

sum of the marginal rate $\frac{dT_1}{dY_1}$ multiplied by the ratio

$$\frac{dY_1}{dY_2} \text{ and } \frac{d(Y_2 - Y_1)}{dY_2}$$